

[\*\*\* high w/ slides on non-Euc geom of conv. ~~\*\*\*~~]

## Riemann

crucial [slides of glossary for R.'s terminology of concepts]

- crucial insight: measurement consists of superposition of magnitudes,  $\rightarrow$  so requiring a new tripartite 'measuring rods' - and the effect of transportation is not something fixed a priori

- crucial insights:

$\exists$  of consistent systems of non-Euc geom show that we cannot assume, as Kant did, that Euc geom is a priori form of intuition - indeed, one cannot even assume that the various combinations of geom axioms is necessary in any sense, or even rec'y consistent

$\Rightarrow$  Kant's analysis of space did not 'dig deep enough' for its starting points; shall must be an entirely general conception of 'magnitude-concepts', which will then reveal the possibilities for sys of 'measure-relations' in space

$\Rightarrow$  role of approximation, inexactitude of measurement in applying geom'l possibilities to phys'k space

# Lecture: Kant of $\phi$ & Sci - Riemann of Helmholtz

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②

## Helmholtz

[should also see Poincaré's characterization of sequences of possible experiences in topologically non-trivial spaces]

quote p.9

⇒ turned Riemann's construction on its head, instead of analytically characterizing possible metric structures of space, determining possible relations in that <sup>ed so possible mechanical constructions, measurements</sup> he rather begins with "mechanical" assumptions and constructs / derives character of possible metric-relations } the relativity of  $\mu$  - priori

"a priori" concepts "constitutive" of space?

- ① positions of points / bodies, w.r.t other staves regarded as 'fixed' is possible to measure  $\Rightarrow$  coords, which vary continuously
- ② possibility of - "rigid body", to compare spatial magnitudes by congruence relation: n.b. this is not intended in possibility of world, don't really respect measurement rules
- ③ rotation does not affect spatial magnitudes

$\Rightarrow$  measure relations are given by a Riemannian metric  
- if we further assume 'free mobility' of bodies, we get spaces of constant curvature

role of visualization, construction of possible exps

fixed char, precise criterion showing  
- shows that Euclidean cannot be shown to be a priori form of spatial intuition: quote from p.3 ad p.11

- n.b. this construction of possible experience in curved, non-Euclidean space does not contradict Kant's account in all aspects, for K. allowed that one can think whatever is not self-contradictory, and it does assume some concept of construction as 'a priori' -

Helmholtz, cont.

but it does show that ~~Kant~~ <sup>one can accept the</sup> idea of a form of intuition that shapes <sup>(additionally)</sup> our possible experiences, but not our possible judgments of possible expers (contra Kant) and that it may not in the event be Euc <sup>(all of)</sup>

$\Rightarrow$  so it can't be a priori in Kant's sense of the term

$\Rightarrow$  but leaves open the possibility to be explored by Reichardt, that it is a priori in a weaker sense

- diff't systems of geom are relatively consistent

- impossibility, when one does not take mechanical considerations into account, of telling whether we live in flat space or in the (space of the) concave reflective surface

$\Rightarrow$  taking mechanical considerations into account may resolve this (shades of Newton)

$\Rightarrow$  seeds of Poincaré's conventionalism about geom of dyn

$\rightarrow$  emphasis on possibilities of diff't sorts of motions, what one requires as background structure to make them possible, harkens back to Newton's analysis of space based on the dynamical requirements of his Laws - but Helm. does it for more generally, sticking to the purely kinematical level